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Economic growth in a super-multiplier model**

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Schumpeter and Keynes: Economic Growth in a Super-Multiplier Model

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Abstract:

We present a model of economic growth that is based on Keynesian ideas (the role of autonomous demand in economic growth) as well as Schumpeterian notions (technological change). Our model fits in the Sraffian supermultiplier (SSM) tradition, and we endogenise the growth rate of autonomous demand, and semi-endogenise productivity growth. The basic model has a steady state that is consistent with a stable employment rate. Consumption smoothing (between periods of high and low employment) by workers is the mechanism that keeps the growing economy stable. We also introduce a version of the model where the burden for stabilisation falls upon government fiscal policy. This also yields a stable growth path, although the parameter restrictions for stability are more demanding in this case.

Keywords: Economic growth model, Sraffian supermultiplier, Research and Development (R&D)

JEL Codes: O41, E11, E12, E62

1. Introduction

The core of Keynesian economics is the rejection of Say's Law, or, phrased in a more positive way, the importance of the demand side of the economy. In macroeconomics, this insight is applied, among other things, to the problem of unemployment (e.g., Mitchell et al., 2019). This is usually done in the context of the business cycle, i.e., without consideration of the long-run growth potential of the economy as expressed, for example, by productivity growth. However, Keynesian approaches to growth also exist, e.g., Kaldor (1957), Pasinetti (1981), Freitas and Serrano (2015) to name only a few (see Blecker and Setterfield 2020 for an extensive overview).

Schumpeterian economics, on the other hand, looks at long-run growth, and in particular the role of technological change in growth. Whether it is in the mainstream tradition (e.g., Aghion and Howitt, 1992), or the evolutionary tradition (Nelson & Winter, 1982), Schumpeterian growth theory usually does not attribute a large role to demand. What a Schumpeterian approach shares with a Keynesian approach is the emphasis on adjustment rather than equilibrium.

Following Dosi et al. (2010) and Meijers et al. (2019), the main idea in this paper is that combining the Keynesian and Schumpeterian approaches to growth can enhance our understanding of the growth process. What Schumpeterians may learn from Keynesians is how demand-side factors may influence the long-run growth path and the adjustment towards it, and how a dynamic macroeconomic steady state may exist with demand as the main economic coordination mechanism rather than price flexibility (Meijers et al., 2019). What Keynesians may learn from Schumpeterians is that without innovation and technological change, demand cannot be a long-run source of growth. The model that we present in this paper intends to bring out these lessons in a clear analytical fashion, and contributing to an existing modelling approach.

Our main interest is to develop a relatively simple analytical model in which both demand (Keynes) and supply (Schumpeter) factors affecting growth can be integrated. We choose the Sraffian supermultiplier (SSM) model of Freitas and Serrano (2015) for this purpose, and we extend the basic SSM model by including employment and productivity. Productivity is semi-endogenised with Research and Development (R&D) as the main driving factor. The central question that the model tries to address is how, and under which parameter settings, demand, both autonomous (i.e., not dependent on current income) and non-autonomous, and productivity growth (the supply-side) will adjust to each other to produce a meaningful and stable steady state growth path.

After this introduction, we present a brief literature review in section 2. Section 3 presents our model. Subsections of Section 3 present the baseline model from Freitas & Serrano (2015), our proposal to endogenise (the growth of) autonomous demand and semi-endogenise technological change (productivity growth), the steady state solutions to our model, stability analysis, and several extensions of our main model, including a rudimentary way to deal with returns to financial investments, and a government stabilisation mechanism. In section 4 we summarise the main arguments. More technical details on the model can be found in three appendices.

2. A brief review of some relevant literature

The Sraffian supermultiplier (SSM) approach is the core of a demand-led growth model initially proposed by Serrano (1995). We opt for using this idea as the core of our model because of the simplicity of the basic equations of the model: because investment is fully endogenised, the role of demand in growth is reduced to a single parameter, which is the growth rate of autonomous consumption demand. The SSM approach was further developed by Bortis (1996) and De-Juan (2005), and eventually developed into a tradition of models with much recent momentum.

The baseline SSM model of Freitas & Serrano (2015) offered a solution to the issue of Harroddian instability with a constant income distribution. In the Freitas & Serrano (2015) version of the SSM, the capacity utilisation rate is a strategic decision of the firms. Firms aim at maintaining a certain degree of idle capacity, allowing them to react under changes in the demand conditions. In the long run, capacity utilisation converges to a long-run constant rate. The model stabilises the relationship between productive capacity and aggregate demand by adjustments of the marginal propensity to invest. Because this propensity is an endogenous variable, it enters the multiplier that determines the short-run level of output, hence the term supermultiplier. In this canonical model, income distribution is determined exogenously, given by the institutions that define the bargaining power between wage- and profit-earners, by customs, and by social norms about the fairness of wages.

In the SSM model, investments follow an accelerator mechanism (capital accumulation induced by income) with no autonomous component. Consumption, on the other hand, has an autonomous and non-autonomous (endogenous) component. The autonomous part of consumption grows at an exogenous growth rate. The short-run level of output adjusts to make savings equal to investment ex-post. In this framework, growth is demand-led not only in the short but also in the long run. Economic growth is equal to the exogenous growth rate of autonomous consumption demand, and capital accumulation (given the equilibrium utilisation rate) converges to this rate.

The recent literature on the SSM has been focusing on implementing new elements to this basic model, such as income distribution, stock-flow consistency, technological dynamics, and also in proposing distinct alternatives to think about the “non-capacity creating” autonomous component of demand. Work on the latter, i.e., the sources of the exogenous rate of autonomous demand that determines the growth rate of the economy, includes workers’ autonomous consumption, financed out of credit (Freitas and Serrano, 2015), as part of the wealth of the workers (Brochier & Silva, 2019), capitalists’ consumption (Lavoie, 2016), subsistence consumption including an unemployment benefits system (Allain, 2019), government expenditures (Allain, 2015), exports (Nah & Lavoie, 2017) and R&D investments (Caminati & Sordi, 2019). All these model expansions consider the autonomous expenditure as an exogenous variable, with the exception of Caminati & Sordi (2019), who endogenise it.

Employment does not receive much attention in the SSM tradition so far, with Palley (2019), Brochier (2020) and Fazzari et al. (2020) as notable exceptions. In the long run, and on average, a stable employment rate requires that the growth rate of labour

productivity plus the growth rate of labour supply matches the rate of growth of output (we will formalise this in the SSM context in the next section). Economic growth in the SSM converges to the growth rate of the autonomous demand component. However, in the basic SSM model, there are no explicit mechanisms to ensure that this rate is or becomes equal to the sum of labour productivity growth and labour supply (the natural/supply rate of growth).

As stated by Allain (2019), the natural rate of growth and the autonomous expenditure growth rate should be the same, and this adjustment takes place in the labour market. With constant labour productivity, a stable employment rate requires that labour supply reacts to changes in labour demand. Fazzari et al. (2020) and Nah & Lavoie (2019) argue that labour supply growth reacts to the employment rate. The natural rate of growth converges to the autonomous expenditure trend.

Another way for adjustment to take place is through (labour) productivity growth. Fazzari et al. (2020), Nah & Lavoie (2017), and Palley (2019) all propose convergence of labour productivity to the exogenous growth rate. The inclusion of productivity growth is often done by adding a Kaldor-Verdoorn learning effect (Allain, 2019; Brochier, 2020; Deleidi & Mazzucato, 2019), in which, because of learning by doing, productivity growth depends (positively) on the capital accumulation rate or on the growth rate of output. However, with the Kaldor-Verdoorn effect, changes in the exogenous component of productivity growth have only a transitory effect on the capital accumulation rate. Kaldor-Verdoorn is neither a necessary nor a sufficient condition to guarantee employment stability.

Another alternative is presented in Palley (2019). In this approach, with fixed labour supply, labour productivity growth makes the natural growth rate converge towards the autonomous expenditure growth in the long run. That is done by adding a sensitivity element of productivity to employment. When the employment rate increases, productivity growth increases, because of learning effects similar to the Kaldor-Verdoorn mechanism, and when the employment rate falls, the productivity growth rate falls accordingly. Fazzari et al. (2020) who also adopt this particular assumption, discuss a host of justifications for it.

On the other hand, our approach assumes that the labour supply is stable, and does not adjust automatically to demand, which is an assumption that we make to keep the model simple and pure (in terms of the stabilisation mechanism). We also assume that productivity growth has its own (Schumpeterian) dynamics. Thus, in our approach, the burden for stabilisation (of employment) falls on the rate of output growth. This means that we will endogenise the rate of growth of autonomous (consumption) demand (following the approach of Brochier & Silva, 2019) and introduce a mechanism (consumption smoothing by workers) that makes this rate adjust to the natural rate of growth.

The SSM model came to the Post-Keynesian debate when Neo-Kaleckian authors started including income distribution to this model (Lavoie, 2016, Allain 2015). Nah and Lavoie (2019) and Cassetti (2017) include a conflict-theory approach of inflation into the SSM, in which workers and firms negotiate over their shares in GDP, and this affects output prices and wages. Those models, however, consider fixed productivity, which is a problem

tacked by Brochier & Silva (2019), who propose including income and wealth distribution using a stock-flow consistent (SFC) framework with endogenous labour productivity. Other efforts to add Stock-Flow consistency (SFC) to the SSM model are in Mandarino et al. (2020) and Brochier (2020). In those models, wealth is distributed between the distinct agents of the system, and consumption out of wealth is included as the key autonomous component. This is also the approach that we will take, albeit in much simplified form, to endogenising the growth rate of autonomous demand. Cassetti (2017) also deals with cost-induced inflation in a SSM-SFC model, but in his model, instead of household consumption, government expenditures is the autonomous spending component that leads growth.

There have been some efforts to add technical progress (and productivity growth) to the SSM framework. Those efforts have added R&D investments as an autonomous demand element. In this sense, as in Caminati & Sordi (2019), endogenous autonomous expenditure (investment in R&D and consumption) grows in line with productivity. Deleidi & Mazzucato (2019) have proposed the idea of an entrepreneurial state, where government R&D is the autonomous expenditure mechanism.

Our approach to including productivity growth (or technological change) is rooted in the neo-Schumpeterian tradition, which mainly looks at technology as a supply phenomenon. In this literature, that draws from the classic work of Schumpeter, the dynamics of technology follows an evolutionary mechanism (Nelson & Winter, 1982). This tradition criticises the static orthodox framework of the general equilibrium and proposes a new theory for economic microeconomic dynamics with innovation as a core factor. The basis of growth resides in the market implementation of new technologies, in a scenario of competition through innovation. The system follows a process of natural selection, in which the best adapted firms remain in the market.

The Neo-Schumpeterian literature, however, should not only focus on the mechanisms that drive innovation. As mentioned by Hanusch & Pyka (2007), it must also focus on the uncertain developments in the socio-economic system, observing the effects of productive transformation also on other aspects (such as the public and monetary aspects) being *“concerned with the conditions for and consequences of a removal and overcoming of the economic constraints limiting the scope of economic development.”* (Hanusch & Pyka, 2007, p.276).

There have been many attempts to include the Schumpeterian literature in the demand-led Keynesian macroeconomics. A central contribution resides on the “Keynes meets Schumpeter” tradition, which was started by Dosi et al. (2010) and further developed into a collection of evolutionary micro-to-macro models. This tradition includes the innovation-imitation dynamics in an economic system with heterogeneous agents (firms, workers, banks and government) using an Agent Based Models. Firms in the capital-goods sector invest in R&D activities, which, under certain probability, may result in innovations, increasing productivity. Firms compete in the market, selling machines to consumption-good firms. These firms then hire workers to produce final goods. The demand for final goods by the workers depends on the employment rate and on government transfers to unemployed workers (acting as a mechanism that stabilises the economy). Demand affects production decisions of the firms, including an element of

effective demand in the model, playing then a role in the growth and distribution pattern. However, the main source of growth is still the supply side, with innovation and technological change, given by R&D activities, being the engine of the system.

Our contribution aims at offering a different solution to the compatibility between a Schumpeterian supply-side dynamics and a Keynesian demand-side framework using a macroeconomic dynamic modelling approach. The starting point is the SSM model, which adds to the Keynesian literature a long-run demand-led growth framework. We extend this model, addressing the issues of productivity growth and employment stability by offering a Schumpeterian alternative. We focus on the convergence between the growth rate of autonomous spending (given by private consumption out of wealth or by government) and the growth rate of labour productivity (given by knowledge, innovation and technical change) in a stock-flow consistent version of the SSM model.

3. The model

3.1. Exogenous growth

Our model follows the Sraffian super-multiplier setup of Freitas & Serrano (2015). We extend their basic model by three variables, after which the model can account for all basic variables of the growth process that we are interested in. Like Freitas and Serrano, we start by modelling investment as a function of the capacity utilisation rate:

$$\dot{h} = h\gamma(u - \mu) \quad (1)$$

Here, γ and μ are parameters, h is the share of investment in GDP, and u is the capacity utilisation rate. The latter is defined as follows:

$$u = \frac{Y}{Y_K}, Y_K = \frac{K}{\nu}$$

where Y is output (GDP) K is the stock of fixed capital, ν is the (fixed) capital-output ratio, and Y_K is full-capacity output.

An important part of the model is how GDP is determined in the short run. This is a Keynesian multiplier process, in which we distinguish between wage-income and profit-income (the original Freitas and Serrano model does not make this distinction). As we will discuss in more detail below, the main purpose for making this distinction is to be able to introduce a stabilisation mechanism, which will keep the economy on a stable employment path. The consumption function thus makes a distinction between the two sources of income:

$$C = \sigma Y c_w + (1 - \sigma) Y c_p + Z_w + Z_p \quad (2)$$

where C is consumption, the parameter c is a marginal consumption rate, σ is the share of wage income in GDP (we will consider this as a parameter, although we would think that further development of the model would endogenise this), Z is autonomous consumption (i.e., independent of current GDP), and the subscripts w and p represent wage income and profit income. We can now derive GDP in the well-known way:

$$Y = C + hY = \sigma Y c_w + (1 - \sigma) Y c_p + Z_w + Z_p + hY \Rightarrow$$

$$Y = (Z_w + Z_p) \frac{1}{1 - \sigma c_w - (1 - \sigma) c_p - h} \quad (3)$$

where $1/(1 - \sigma c_w - (1 - \sigma) c_p - h)$ is the supermultiplier.

To make our model resemble that of Freitas and Serrano, we can assume $c_w = c_p \equiv c$ and define $1 - c \equiv s$. We then also drop the distinction between Z_w and Z_p , and denote total autonomous consumption by Z . Then the supermultiplier becomes $1/(s - h)$ and equation (3) reduces to

$$Y = Z \frac{1}{s - h} \quad (4)$$

Writing the growth rate of Z as $g_Z \equiv \dot{Z}/Z$ (a dot above a variable will denote a time derivative), and still referring to the reduced (Freitas and Serrano) version of the model, we can write the growth rate of GDP in the following way:

$$\frac{\dot{Y}}{Y} \equiv g = g_Z + \frac{h}{s - h} \quad (5)$$

This equation allows us to return to the growth context of the model. The original Freitas and Serrano model consists of two equations: (1) and a differential equation for the capital utilisation rate u . By its definition, the growth rate of u is equal to the growth rate of GDP (g as in 5) minus the growth rate of the capital stock. We denote the latter as $g_K \equiv \dot{K}/K$. Like Freitas and Serrano, we assume that capital accumulation is a perpetual inventory process, with a fixed depreciation rate δ :

$$\dot{K} = I - \delta K = hY - \delta K \Rightarrow g_K = \frac{hu}{v} - \delta \quad (6)$$

With this, we can write the differential equation for the capacity utilisation rate:

$$\frac{\dot{u}}{u} = g - g_K = g_Z + \frac{h}{s - h} - \frac{hu}{v} + \delta \quad (7)$$

As we are interested not only in the capacity utilisation rate but also in employment, we will derive a similar expression for the employment rate, which we will denote by E . We will assume a constant labour force and a fixed labour coefficient in the short run, i.e., $a = Y/L$, where a is labour productivity. We will allow for labour productivity to grow over time, and will set $\dot{a}/a \equiv \rho$. Then

$$\frac{\dot{E}}{E} = g - \rho = g_Z + \frac{h}{s - h} - \rho \quad (8)$$

If we consider g_Z and ρ as exogenous, we already have a full model that consists of equations (1), (7) and (8), with variables h , u , and E . In the steady state of this model, equation (1) dictates that $u = \mu$ so that $\dot{h} = 0$, and it follows (from equations 7 and 8) that $\dot{u}/u = g_Z - g_K$ and $\dot{E}/E = g_Z - \rho$. This implies that for any steady state values of u and E to exist, we must have

$$g_Z = g_K = \rho \quad (9)$$

In this equation, which is in line with the analysis in Palley (2019) and Fazzari et al. (2020), g_K is endogenous, but (so far) g_Z and ρ remain exogenous. If, like Freitas and Serrano, we set $\rho = 0$, and disregard equation (8) (i.e., do not consider employment to be a variable of interest), then equation (7) solves for $h = (g_Z + \delta)v/\mu$. In this case, g_K will adjust to become equal to g_Z .

Equation (9) shows that if we wish to consider employment in this context, and if we wish to have a (positive) steady state value for the rate of (un)employment, then we must assume that the two exogenous growth rates are equal to each other ($\rho = g_Z$). Then g_K will adjust to become equal to $\rho = g_Z$. However, if $\rho \geq g_Z$, and with both of these rates exogenous, there is no change of a steady state with both capital utilisation and employment constant (and positive).

Because there is no a priori good reason why in a model of exogenous growth $\rho = g_Z$, we proceed to endogenise both these rates. We will investigate models in which ρ is semi-endogenised, and in which g_Z is fully endogenised. The (semi)-endogenisation of ρ will take inspiration from Schumpeterian thinking, while for the endogenisation of g_Z will draw upon the idea of consumption smoothing by workers (as the variety of our model), or government fiscal policy (in an alternative model version). Given our choices on endogenisation, a stable steady state results if g_Z is endogenised, even if we leave ρ completely exogenous.

3.2. Semi-endogenising ρ

In the model with semi-endogenous productivity growth, we start by assuming that a share τ of GDP is spent (out of profit income) on Research and Development (R&D). We consider τ as an exogenous parameter, but propose that further development of the model would endogenise this parameter.

With R&D included in the model, equation (3) changes to

$$Y = (Z_w + Z_p) \frac{1}{1 - \sigma c_w - (1 - \sigma) c_p - \tau - h} \quad (3a)$$

Further, we define the ratio of the R&D-capital stock to the stock of fixed capital as $\Phi \equiv R/K$. R&D-capital (denoted by R) evolves as a stock in the same way as fixed capital K , with a fixed depreciation rate Δ (for most of our steady state calculations, we will assume $\Delta = \delta$, i.e., R&D capital and fixed capital depreciate at the same rate, which will simplify the mathematics):

$$\dot{R} = \tau Y - \Delta R \Rightarrow \hat{R} \equiv \frac{\dot{R}}{R} = \frac{\tau u}{\Phi v} - \Delta \quad (10)$$

Using (6) and (10), we get

$$\dot{\Phi} = \Phi \left(\frac{\tau u}{\Phi v} - \Delta - \frac{hu}{v} + \delta \right) = \Phi \frac{u}{v} \left(\frac{\tau}{\Phi} - \Delta - h + \delta \right) \quad (11)$$

Finally, we assume that productivity growth results from R&D, more specifically, from the value of Φ :

$$\rho = \bar{\rho} + \varphi\Phi \quad (12)$$

where $\bar{\rho}$ (the exogenous part of productivity growth) and φ are parameters. Note that if we set $\tau = 0$, it follows that $\Phi = 0$, or if we set $\varphi = 0$, we are back in the realm of completely exogenous productivity growth ($\rho = \bar{\rho}$).

3.3. Endogenising g_Z : private spending

The first idea that we will employ for endogenising g_Z is that private autonomous consumption depends on accumulated wealth. This is the foundation of the first (and main) model that we present, while in a later subsection we will consider government fiscal policy as another source of endogenous autonomous spending in the economy in an alternative model.

In the appendix, we present a model where, in line with the general consumption function (2), we distinguish between consumption out of wage income as well as profit income, and accumulated wealth is also from wage income and accumulated wealth from profit income. For clarity in exposition, here, in the main text, we will focus on a special case, where there is no consumption out of profit income, nor out of accumulated wealth out of profits. In other words, only wage income and the accumulated savings out of wage income are used for consumption. In this special case, the basic outcomes of the model in terms of growth are unchanged, and the formal expressions for steady state values are significantly simplified relative to the general case.

The basic idea for endogenising g_Z is taken from Brochier (2020), and states that autonomous consumption is dependent on accumulated wealth. In the specific case that we consider here in the main text, this wealth is defined as accumulated savings purely out of labour income (wages). The appendix deals with the more general model in which also accumulated wealth out of profit income is considered.

We denote accumulated savings out of labour income by W_w , and specify its motion by the following equation:¹

$$\dot{W}_w = (1 - c_w)\sigma Y - Z_w - \delta W_w \quad (\text{A2a})$$

The first part of the right-hand side $((1 - c_w)\sigma Y - Z_w)$ simply represents savings out of current labour income. The term $-\delta W_w$ represents depreciation of wealth. This arises from the specific setup of the model, explained in more detail in the appendix, in which total accumulated wealth in the economy is equal to the sum of the productive capital stocks (both R&D capital R and fixed capital K). In this way, W_w is seen as an entitlement of the holders (wage earners) on the stock $R + K$. The term $-\delta W_w$ is included because the entitlement to $R + K$ will depreciate with the stocks themselves, and we assume, for simplicity, that R&D capital and fixed capital depreciate at the same rate $\Delta = \delta$.

¹ Equation numbers starting with A refer to one of the three appendices. These equations are introduced and discussed in some detail in the appendices, in this case the context of the model with generalized consumption function.

The general model has a corresponding wealth variable W_p , which represents assets held by profit earners. As the appendix shows, $W_w + W_p = R + K$. Because of the specific assumptions made here (no autonomous consumption out of W_p), we do not need the variable W_p in the exposition in the main text. However, we do have to introduce the variable $x \equiv W_w / (W_w + W_p) = W_w / (K + R)$, which represents the share of wage earners in total wealth of the economy.

The endogenisation of g_Z then proceeds by positing

$$Z_w = \zeta_w W_w \quad (\text{A4a})$$

$$Z_p = \zeta_p W_p \quad (\text{A4b})$$

Here ζ_w is a new variable that represents the (marginal) propensity to consume out of accumulated workers' savings, and similarly ζ_p is a parameter that represents the marginal propensity to consume out of profit earners' assets. Note that we assume $\zeta_p = 0$ (as well as $c_p = 0$) in the main text, i.e., equation (A4b) is only reported here for completeness (these assumptions are relaxed in Appendix 1). Our assumption is also that the variable ζ_w is a behavioural variable that serves to smooth (autonomous) consumption spending for changes in workers' income that result from changes in the employment rate. More specifically, we specify

$$\dot{\zeta}_w = \iota \zeta_w (\bar{E} - E) \quad (13)$$

Here ι and \bar{E} are parameters (both >0). \bar{E} specifies a neutral rate of employment at which ζ_w does not change. Below (above) this employment level, ζ_w increases (decreases) to make up for lost (gained) wage income relative to the neutral level. Equation (13) is a key mechanism in our model that proves to provide stability to the growth path in terms of ensuring a stable employment rate.

The ultimate model (with semi-endogenised ρ and fully endogenised g_Z) contains six variables: h, u, E, Φ, ζ_w and x . We have already specified differential equations for h, Φ and ζ_w (equations 1, 11 and 13, respectively). We also have general forms (equations 7 and 8) for the differential equations for u and E , in which we still need to specify the endogenised variable g_Z . We also need to specify the differential equation for x .

Let us start by writing the expression for g_Z , which will give us two differential equations. Clearly, from equation (A4a), $g_Z = (\dot{\zeta}_w / \zeta_w) + (\dot{W}_w / W_w)$. The first of the terms on the righthand side of this follows directly from equation (13). With the assumption that autonomous consumption out of profit income is zero, we can also write

$$g_W \equiv \frac{\dot{W}_w}{W_w} = \zeta_w x \left(\frac{\tau+h}{1-c_w \sigma - \tau - h} \right) - \delta \quad (14)$$

(This equation is a specific case of equation A6). This leads to

$$g_Z = \iota (\bar{E} - E) + \zeta_w x \left(\frac{\tau+h}{1-c_w \sigma - \tau - h} \right) - \delta \quad (15)$$

(the more general form of this is A7).

And then:

$$\dot{u} = u \left(\iota(\bar{E} - E) + \zeta_w x \left(\frac{\tau+h}{1-c_w\sigma-\tau-h} \right) + \frac{\dot{h}}{1-c_w\sigma-\tau-h} - \frac{hu}{v} \right) \quad (7')$$

$$\dot{E} = E \left(\iota(\bar{E} - E) + \zeta_w x \left(\frac{\tau+h}{1-c_w\sigma-\tau-h} \right) + \frac{\dot{h}}{1-c_w\sigma-\tau-h} - \delta - \bar{\rho} - \varphi\Phi \right) \quad (8')$$

Finally, we can derive the last differential equation from the definition $x = W_w / (W_w + W_p)$:

$$\dot{x} = \frac{(\zeta_w x + \zeta_p(1-x))((1-c_w)\sigma - x(\tau+h))}{1-c_w\sigma - c_p(1-\sigma) - \tau - h} - \zeta_w x \quad (16)$$

3.4. Steady state

In this section, we will analyse the steady state of the model with semi-endogenous productivity growth and endogenous g_Z as specified in the previous section (i.e., private autonomous spending as the source of g_Z). We will ignore the trivial steady state solution where all variables are zero

We can start by setting equations (1) and (13) to zero, which immediately yields $u^* = \mu$ and $E^* = \bar{E}$ (we will denote steady state solutions by a * superscript). Next, setting equations (7') and (8') to zero, re-arranging and equating the results of both equations, as well as substituting (15), yields the following quadratic equation for Φ :

$$\varphi\Phi^2 + (\delta + \bar{\rho})\Phi - \frac{\tau\mu}{v} = 0 \quad (17)$$

Obviously, this equation has two solutions, but only one of them yields a positive value for Φ :

$$\Phi^* = \frac{-(\delta + \bar{\rho}) + \sqrt{(\delta + \bar{\rho})^2 + \frac{4\varphi\tau\mu}{v}}}{2\varphi} \quad (18)$$

To derive the steady state value for h , two routes are now open. One of these is to set equation (11) to zero, which yields (remember we assume $\Delta = \delta$ for simplicity):

$$\dot{\Phi} = \Phi \frac{u}{v} \left(\frac{\tau}{\Phi} - h \right) = 0 \Rightarrow \frac{\tau}{\Phi^*} = h^* \quad (19)$$

Equation (18) could be substituted into (19) to obtain h^* as a function of only parameters. The other route is to set (7') and (8') to zero, solve each of these for ζ_w and equate the two expressions, which yields

$$h^* = \frac{v}{\mu} (\delta + \bar{\rho} + \varphi\Phi^*) \quad (20)$$

Again, we can substitute (19) to obtain an (alternative) expression for h^* as a function of only parameters. Equation (20) also shows that the steady state value for the investment rate h depends on the rate of technological change (or productivity growth): as productivity growth rate is faster, capital needs to accumulate at the same rate (see equation 9), which requires a higher value of h .

However, rather than actually presenting either one of these expressions (which are equivalent), we show in Figure 1 how the parameter τ influences the simultaneous

determination of the steady state solutions Φ^* and h^* , as well as the resulting rate of productivity growth, ρ . The figure shows that all three of these steady state outcomes are concave functions of τ . In other words, increasing the rate of R&D spending as a fraction of GDP will have a positive but declining effect on the steady state values of the investment rate (h), the ratio of the R&D stock to the stock of fixed capital (Φ), and, as a result of the latter, the rate of productivity growth.

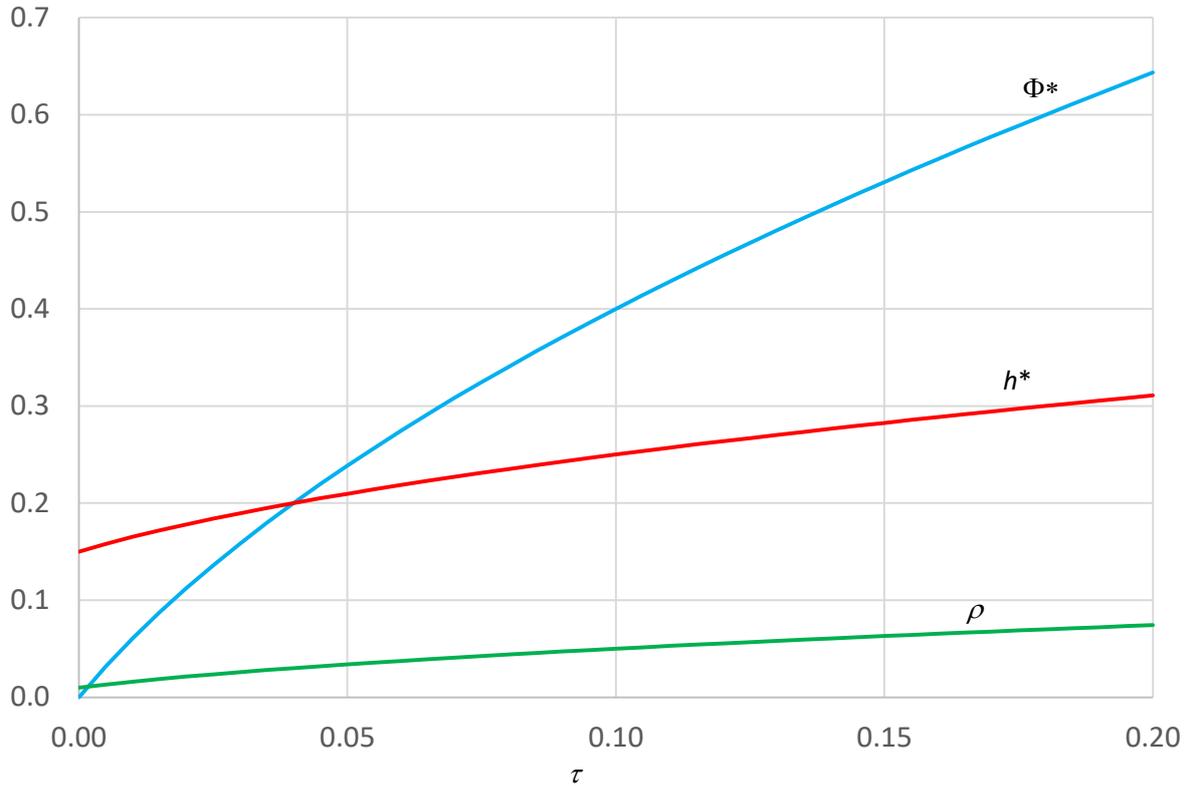


Figure 1. Steady state values of Φ , h and ρ as a function of τ

Next, we set equation (16) to zero, solve for ζ_w and equate this to the expression for ζ_w that can be derived from setting (8') to zero. This yields the steady state solution for x :

$$x^* = 1 - \frac{(1-\sigma)}{(\tau+h^*)} \quad (21)$$

Obviously, the denominator of the fraction on the right-hand side ($\tau + h^*$) is the fraction of GDP that needs to be invested (in fixed capital and R&D) in the steady state. The higher this share is, the more firms need to borrow from workers to fund investment, and hence the higher the steady state value of x .

Finally, we can use any of the expressions that were derived for ζ_w and substitute x^* to obtain

$$\zeta_w^* = \frac{(1-\sigma c_w - (\tau+h^*))h^{*\frac{\mu}{\nu}}}{(\tau+h^*)-(1-\sigma)} \quad (22)$$

In this expression, as long as $\tau + h^* < 1$, σ has a negative effect on ζ_w^* (the higher the share of wages in GDP, the lower the resulting rate of autonomous consumption spending). The effect of τ is also negative, which is in line with our conclusion on equation (21) (the higher τ , the more firms tend to borrow). The effect of h^* is harder to isolate, but it appears to be negative, with the same intuition as the effect for τ .

With all steady state values of the endogenous variables derived, we are able to look at how growth works in this model. Equation (9) states that $g_Z = g_K = \rho$, and we also know that in the steady state the growth rate of GDP (g) is equal to this. Using equation (12), we see that in the steady state $\rho = \bar{\rho} + \varphi\Phi^*$, and equation (18) shows that Φ^* depends on a range of parameters, which includes δ , τ , μ , and v ($\bar{\rho}$ and φ were already included).

All of these are supply-side parameters, and some (τ , $\bar{\rho}$ and φ) can be considered to be Schumpeterian parameters, as they relate to the process of technological change. Demand-side parameters, such as c_w , \bar{E} or even σ do not enter the expression for the long-run growth rate of the economy. What happens is that g_Z (the demand side) adjusts to the growth rate of productivity. This also implies that the endogenisation of the demand side (g_Z) is crucial for the existence and stability of a steady state. In fact, we could keep the rate of productivity growth completely exogenous (e.g., $\varphi = 0$), and, as long as we keep the endogenisation of g_Z , the steady state of the model would still exist.

In the next section, we will consider whether demand side adjustment can produce a stable path towards the steady state values that we derived. Before we undertake to answer this question, we can also note that the general model, for which we document the steady state expressions in the appendix, arrives at the same conclusion with regard to the unique importance of the supply side in determining the growth rate. In other words, also if we relax the assumption that only wage earners consume, we see no change in the steady state growth rate of the economy. Only the steady state values of x and ζ_w will change if we relax those assumptions.

3.5. Stability analysis

We used numerical simulations to explore the behaviour of the model as specified so far. These simulations were done in R, using the `ssmod` function, which numerically integrates the equations. Figure 2 documents the time paths for the variables of the model in the baseline simulation, which uses the following parameter values: $\tau = 0.05$, $\delta = 0.05$, $v = 2$, $\mu = 0.8$, $\bar{E} = 0.8$, $c_w = 0.6$, $\sigma = 0.8$, $\varphi = 0.1$, $\bar{\rho} = 0.01$, $\iota = 0.85$, $\gamma = 0.15$ as well as $c_p = 0$ and $\zeta_p = 0$ which we assumed throughout the main text so far. We see that, for these parameter values, the model converges (with dampened fluctuations) to the steady state.

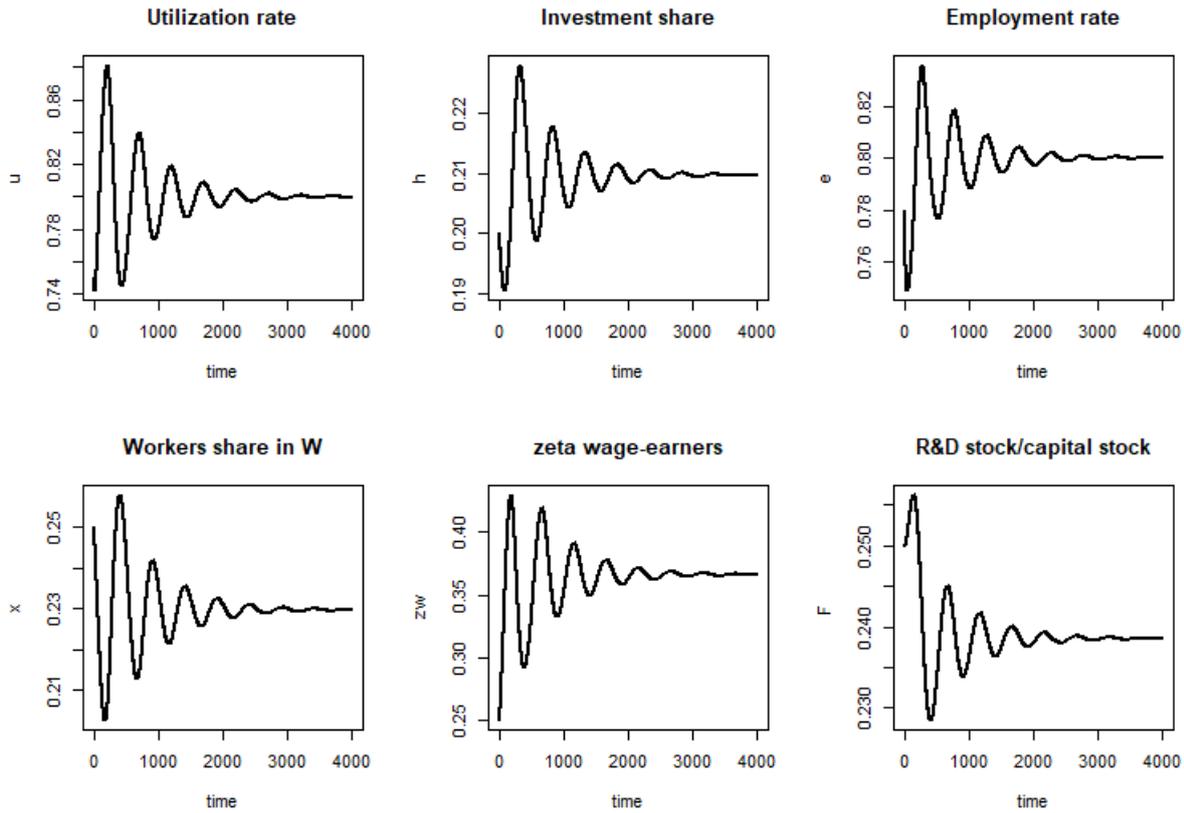


Figure 2. Model simulation showing stability of the steady state

In order to obtain a more comprehensive overview of stability, we used Matlab's symbolic math toolbox to derive the Jacobian matrix corresponding to the model. This enables us to do a grid search of parameter space, and numerically calculate the eigenvalues of the Jacobian matrix at the steady state, for each particular parameter constellation. With 11 (or even 13) parameters, it is impossible to do a complete search. Therefore, we limited our search of parameter space to just 5 parameters, which are τ , σ , c_w , ι and γ . The other parameters are fixed at the values listed above.

The parameter grid search not only gives information about stability of the steady state. It also provides insights into the sign of some of the steady state values of the variables. In the broad and coarse grid search that we implemented², it appeared that there are parameter sets in which either x or ζ_w (or both) are negative (and stable). While such negative values are not impossible to interpret (essentially, they represent an indebted working class), we will focus on parameter values that yield positive values for x and ζ_w . The parameter grid search suggests that we need fairly high values of σ (typically 0.75 or higher for the restricted model of the main text) and τ (typically 0.05 or larger) to ensure this. Relaxing the assumption that profit earners do not consume reduces the likelihood of negative steady state values for x or ζ_w considerably. The key parameter to relax this

² We analysed the following ranges in this broad and coarse grid search τ : 0.01 – 0.07; σ : 0.5 – 0.9; c_w : 0.4 – 0.9, ι : 0.01 – 1.5; and γ : 0.01 – 0.25.

assumption is ζ_p . If we set $\zeta_p = 0.15$, values of $\sigma = 0.7$ or lower still generate positive values for x and ζ_w .

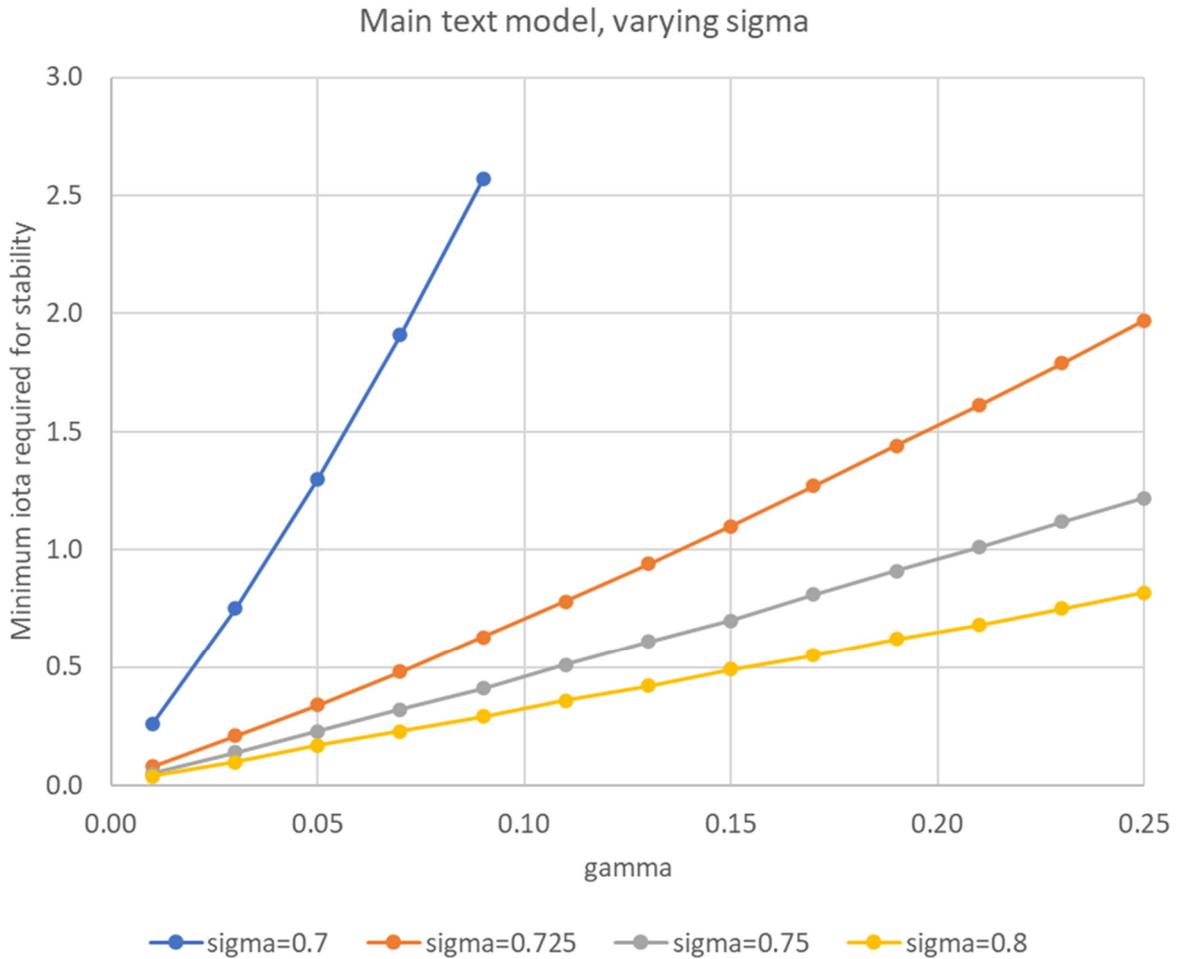


Figure 3. The role of parameters γ and ι in the main model for stability of the steady state

Inspection of the results of the grid search suggests that the parameters ι and γ play a crucial role in stability. In particular, we need a minimum value of the ratio ι/γ for the steady state to be stable. This is illustrated in Figure 3, which documents, for different (and fixed) values of the parameters other than ι and γ , on the vertical axis the minimum value of ι that yields a stable steady state given the value of γ on the horizontal axis.³ For example, the grey line (which is drawn for a value $\sigma = 0.75$) shows that if $\gamma = 0.15$, stable steady state values are obtained for values of $\iota \geq 0.7$. All lines in the figure are (approximately) linear, which means that along each line, the ratio ι/γ is fixed, and we need this ratio to be larger than the slope of the line for the model to have a stable steady

³ A stable steady state, in this case means that all eigenvalues (of the Jacobian matrix evaluated at the steady state) are either non-imaginary and negative, or imaginary with a negative real part. We also checked for zero real (parts of) eigenvalues, but this did not happen in the cases we considered.

state. This implies that ι needs to be relatively large for stability, and that larger values of γ require larger values of ι .

The figure also provides different lines for varying values of σ . These indicate that the lower σ is (e.g., the blue line represents the lowest value of σ that we considered here, 0.7), the higher the required ratio ι/γ is. Given γ , higher values of pose lower restrictions on ι for stability. For example, the individual simulation run that we documented above (with $\sigma = 0.8$, $\gamma = 0.15$ and $\iota = 0.85$) lies well above the yellow line.

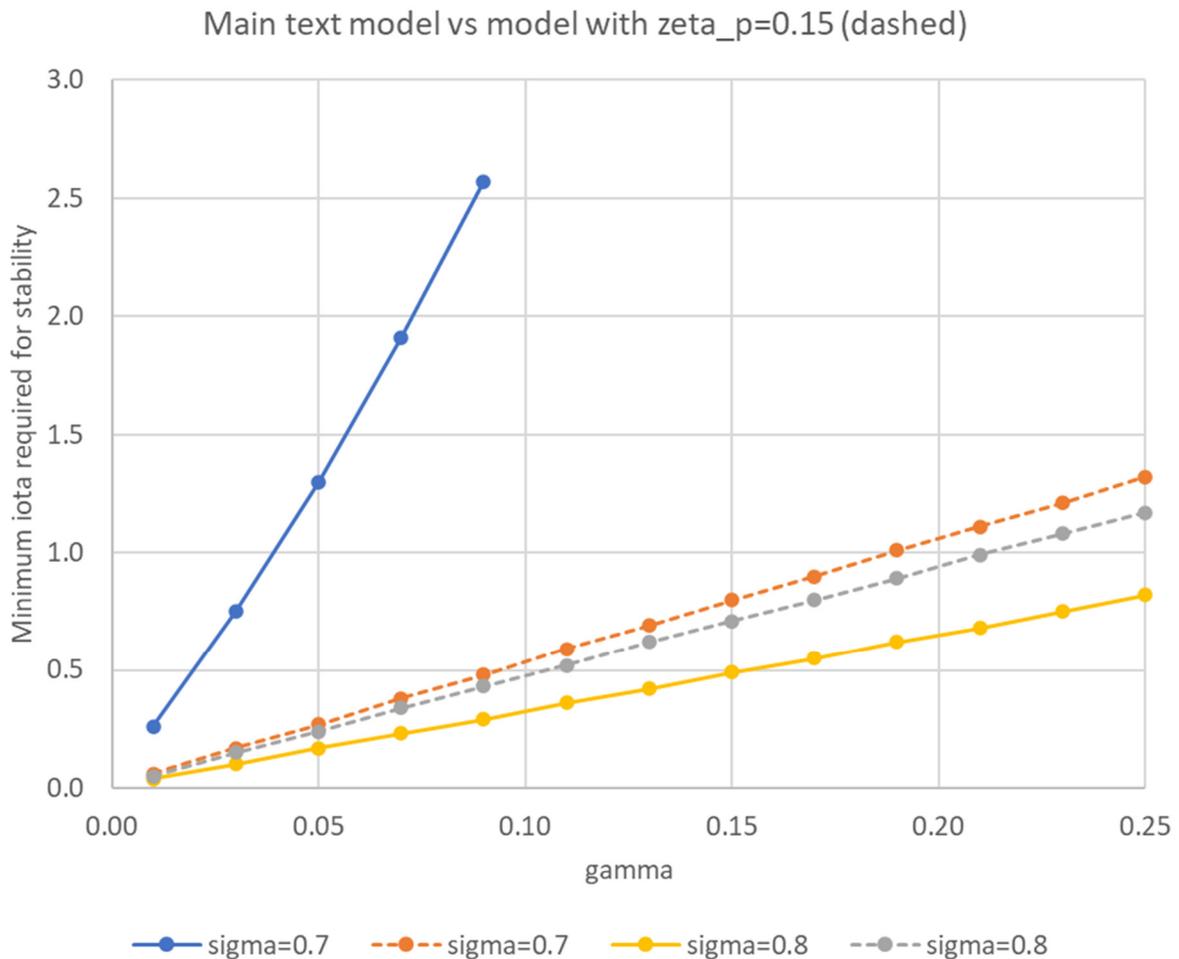


Figure 4. The role of parameters γ and ι in the main model with zero and positive ζ_p for stability of the steady state

Figure 4 documents similar results, but now comparing to a more general case where we relax the assumption $\zeta_p = 0$ and instead set $\zeta_p = 0.15$ ($c_p = 0$ remains as an assumption). Here we only consider the ‘extreme’ values $\sigma = 0.8$ and $\sigma = 0.9$, i.e., the blue and yellow curves are the same as in the previous figure. Interestingly, compared to the case $\zeta_p = 0$, $\zeta_p = 0.15$ moves the lines ι/γ much closer together. This means that with $\zeta_p = 0.15$, differences in σ matter much less for stability than in the case $\zeta_p = 0$. The intuition for

this result lies in the variable x . Because profit earners now consume out of their wealth, their share of total assets in the economy decreases, i.e., the steady state value for x increases. With a larger base for their autonomous consumption, consumption smoothing becomes easier for workers, which makes ι a less crucial parameter for stability.

3.6. Introducing a rate of return to accumulated savings

So far, we have assumed that there is no return on the accumulated savings by workers. This is, of course, an unrealistic assumption. Ideally, the model that we presented so far would be extended to include a financial market, which would offer various instruments that could be used to invest savings. Such a financial sector would also have to include additional agents, such as a government, a central bank and private banks. While the tradition of so-called stock-flow-consistent models (Godley and Lavoie, 2007; Brochier & Silva, 2019) offers such models, we leave the extension of our model in this elaborate way to future work. Instead, we opt here for a very rudimentary way of incorporating a rate of return.

Our main idea, which we already briefly referenced above, is that accumulated workers' savings can be seen as a claim on the production factors that are accumulated in firms, i.e., fixed capital and knowledge capital (R&D). Remember that total assets (aggregated over workers and profit earners) in the economy are equal to the sum of the capital stock and the R&D stock. Workers' assets (accumulated savings) are a share of this (which is the variable x), and our equations will specify that workers are entitled to a proportional share of current profits.

Such an allocation of part of profit income to workers means that workers now receive more (if $x > 0$) than the share σ of GDP. If this redistribution would be completely proportional, workers would receive a share $\sigma + x(1 - \sigma)$, and profit earners a share $(1 - x)(1 - \sigma)$. However, we introduce a new parameter, $0 \leq r \leq 1$, which measures the extent to which profits are redistributed. With the inclusion of this new parameter, workers will receive a share $\sigma + rx(1 - \sigma)$ of GDP, and profit earners a share $(1 - \sigma)(1 - rx)$. It is easily seen that if $r = 0$ (i.e., no returns on accumulated savings), we have the model as it has been presented so far, while if $r = 1$, we have the expressions as firstly introduced in this paragraph (returns fully proportional to x).

The marginal propensities to consume (or save) for workers and profit earners are applied to total income, i.e., to the shares of GDP as specified in the previous paragraph. This changes some of the equations in the model, and this is documented in full detail in Appendix 2. Here, we only summarise the main result of this change, which solely lies in the steady state values for the variables x and ζ_w . The steady state expressions are given in the appendix. Generally, for $r > 0$, we find larger steady state values for x as compared to equation (21), or its more general counterpart found in Appendix 1 (equation A12). For the case $r = 1$, we find $x^* = 1$, i.e., workers own the entire capital stock. For all cases $r < 1$, $x^* < 1$ remains, thus as long as profit-earners are left with some of the current-period profits, they will always be able to accumulate at least some level of positive assets. However, when $r = 1$, and independently of how much they save, the savings of the profit

earners become insufficient to compensate for the depreciation on the physical assets they hold.

The positive effect on x^* in cases $r > 0$ has implications for stability. This is shown in Figure 5, which is similar to the two previous figures. Here all lines are drawn for $\sigma = 0.8$. The solid line is the case of the model of the main text, i.e., $\zeta_p = 0$, which yields the same line as already shown in the previous two figures. The dashed grey line assumes $\zeta_p = 0.15$ but keeps $r = 0$, and hence this is the same line as in the previous figure. The other two lines introduce two new cases: $r = 0.5$ (green) and $r = 1$ (red). We can see that a higher value of r shifts the ι/γ tradeoff line down, i.e., increases stability. This is the same effect as observed before: the increase in x^* makes consumption smoothing easier to implement for given ι .

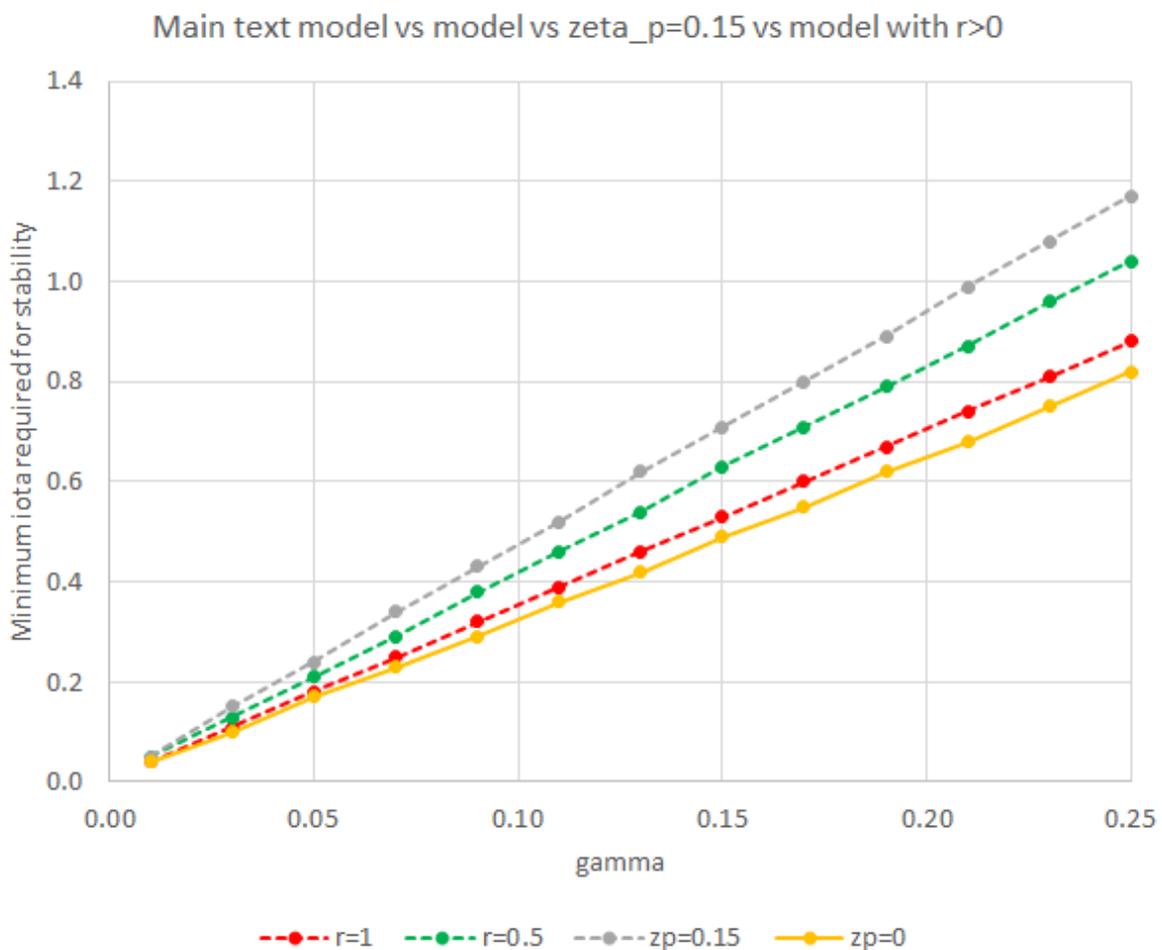


Figure 5. The role of parameters γ and ι in the model with a financial return for stability of the steady state

3.7. Endogenising g_Z : government spending

We conclude our model analysis by considering an alternative mechanism for stabilising the economy. Whereas so far private autonomous consumption spending worked as a stability mechanism by workers' desire to smooth consumption between periods of high

and low unemployment, we now ask whether the government is able to stabilise the economy by fiscal policy. Here, we will discuss the changes that are made to the model of the previous sections to analyse this question. Full details of some of the equations of the model with government fiscal policy are provided in Appendix 3.

In order to consider the model with a government, we will make one major simplification to the model as considered so far: we will no longer distinguish between workers and profit earners in the private sector. This means that the variable x is no longer relevant, and that we have only a single parameter for the marginal consumption rate (we will denote this parameter by c), and a single variable for autonomous spending by the private sector (this variable will be denoted as Z_h). As before, Z_h will be a fraction (denoted by ζ_h) of total private-sector assets (or wealth). Because our focus is on the government sector as a stabilisation mechanism, we will assume that ζ_h is a fixed parameter.

On the other hand, the introduction of a government sector also means that we have to introduce new variables and equations into the model. The first of these variables is Z_G , which is autonomous government (consumption) spending. Another variable is the tax rate T , which is specified as a share of GDP, which implies that TY is total tax revenue. We also specify total outstanding government debt, which we denote by G .

In line with the previous section, we assume that the government has to pay interest on the bonds that it issues to fund outstanding debt G . For simplicity, we assume that this rate of return is equal to the private rate of return on invested capital (R&D capital R and fixed capital K). We then consider profit income as the return on invested capital, which means that the rate of return is equal to $(1 - \sigma)Y/W$, where σ is, as before, the parameter that represents the share of wages in GDP, and hence $(1 - \sigma)$ is the share of profits. W denotes the total invested capital by private agents, which in the model of the previous sections was split into W_w and W_p . Because we have now assumed a fixed ζ_h , we have $W = W_w + W_p = R + K$, where W_w and W_p are variables that are only relevant for the comparison with the model of the previous sections.

Finally, we introduce a new variable $D \equiv G/W$, which is government debt as a share of $W = R + K$. With the interest rate on government bonds equal to $(1 - \sigma)Y/W$, total interest payments (to the public, which holds the bonds) are equal to $G(1 - \sigma)Y/W = (1 - \sigma)DY$. Then we have

$$\dot{G} = Z_G + (1 - \sigma)DY - TY = Z_G + Y((1 - \sigma)D - T) \quad (23)$$

and

$$\dot{D} = \zeta_G + \frac{[(\zeta_H + \zeta_G) + \zeta_H D][D(1 - \sigma - h - \tau) - t]}{1 - c(1 - t + (1 - \sigma)D) - (h + \tau)} + D\delta \quad (24)$$

The government model needs a number of behavioural equations for the government. First, we assume that government spending is proportional (by ζ_G) to the private wealth variable W :

$$Z_G = \zeta_G W \quad (A4d)$$

We then also need a behavioural rule for the spending fraction ζ_G :

$$\dot{\zeta}_G = \zeta_G \iota_G (\bar{E} - E) \quad (13a)$$

This is similar to the rule that we used for workers' consumption smoothing in the previous sections (equation 13), but here it is the government who takes this task upon itself. The main difference is that the government needs to borrow money to perform this function, whereas workers could draw on their savings. Hence the government raises taxes to fund its debt, and therefore we need a behavioural rule for the tax rate. Here, we will assume that the government sets a long-run neutral value for the variable D , and adjusts the tax rate to maintain this value (in the long run):

$$\dot{T} = T\eta(D - \bar{D}) \quad (25)$$

In what follows, we will set \bar{D} (the neutral D value) to zero, which means that the government aims to have no debt in the long run (the model that we analyse is a balanced budget supermultiplier model). This is a strict assumption, which we make for mathematical convenience, but assuming $\bar{D} > 0$ does not fundamentally change the conclusions.

This concludes the model with government stabilisation. The model consists of seven endogenous variables: h , Φ , u , E (all of which were present in the model without a government), T , D , and ζ_G . The differential equations for h and Φ are unchanged, they are (1) and (11), respectively. The differential equations for u and E are slightly changed and are specified by substituting the new expression for g_Z (equation A7a in Appendix 3) into the generic forms (7) and (8). These two equations are documented as (7a) and (8a) in Appendix 3. Finally, equations (25), (24) and (13a) provide the differential equations for the new variables T , D , and ζ_G .

3.8. Steady state and stability

The (non-trivial) steady solution of the model can be derived in the same way as was done for the model without a government. The expressions for h^* , Φ^* , u^* and E^* do not change from what we had without a government, which leaves only the three new government-related variables. We leave details of the derivations of the steady state values of these variables to the interested reader, and just document these values:

$$D = \bar{D} = 0 \quad (26)$$

$$\zeta_G^* = \frac{\mu}{v(1+\Phi^*)} - \frac{(\delta + \bar{\rho} + \varphi\Phi^*) + \zeta_h}{(1-c)} \quad (27)$$

$$T^* = 1 - \frac{v(1+\Phi^*)}{\mu} \frac{(\delta + \bar{\rho} + \varphi\Phi^*) + \zeta_h}{(1-c)} \quad (28)$$

We simulate this model with the following parameter values: $\tau = 0.075$, $\delta = 0.05$, $v = 2$, $\mu = 0.8$, $\bar{E} = 0.8$, $c = 0.6$, $\sigma = 0.7$, $\varphi = 0.1$, $\bar{\rho} = 0.01$, $\iota_G = 0.95$, $\gamma = 0.1$, $\zeta_h = 0.01$, and $\eta = 0.1$. Figure 6 shows how, under these parameter values, the model converges to the steady state with dampening oscillations. Along the adjustment path, the variable D also takes negative values, i.e., at some times, the government borrows money from the private sector.

Note that in the set of parameter values that we chose, ι_G is quite a bit larger than η . It makes intuitive sense that this is a condition for government fiscal policy to be an effective stabiliser. Obviously, the primary stabilisation mechanism is ζ_G , which adjusts in response to (un)employment (equation 13a). On the other hand, equation (25), which determines the dynamic path of the tax rate, works against such stabilisation, because a higher tax rate will decrease private consumption. Thus, any positive effects on GDP and employment from increasing ζ_G will be offset by an increasing tax rate. If the tax effect is immediate, fiscal policy will become ineffective in stabilising the economy.

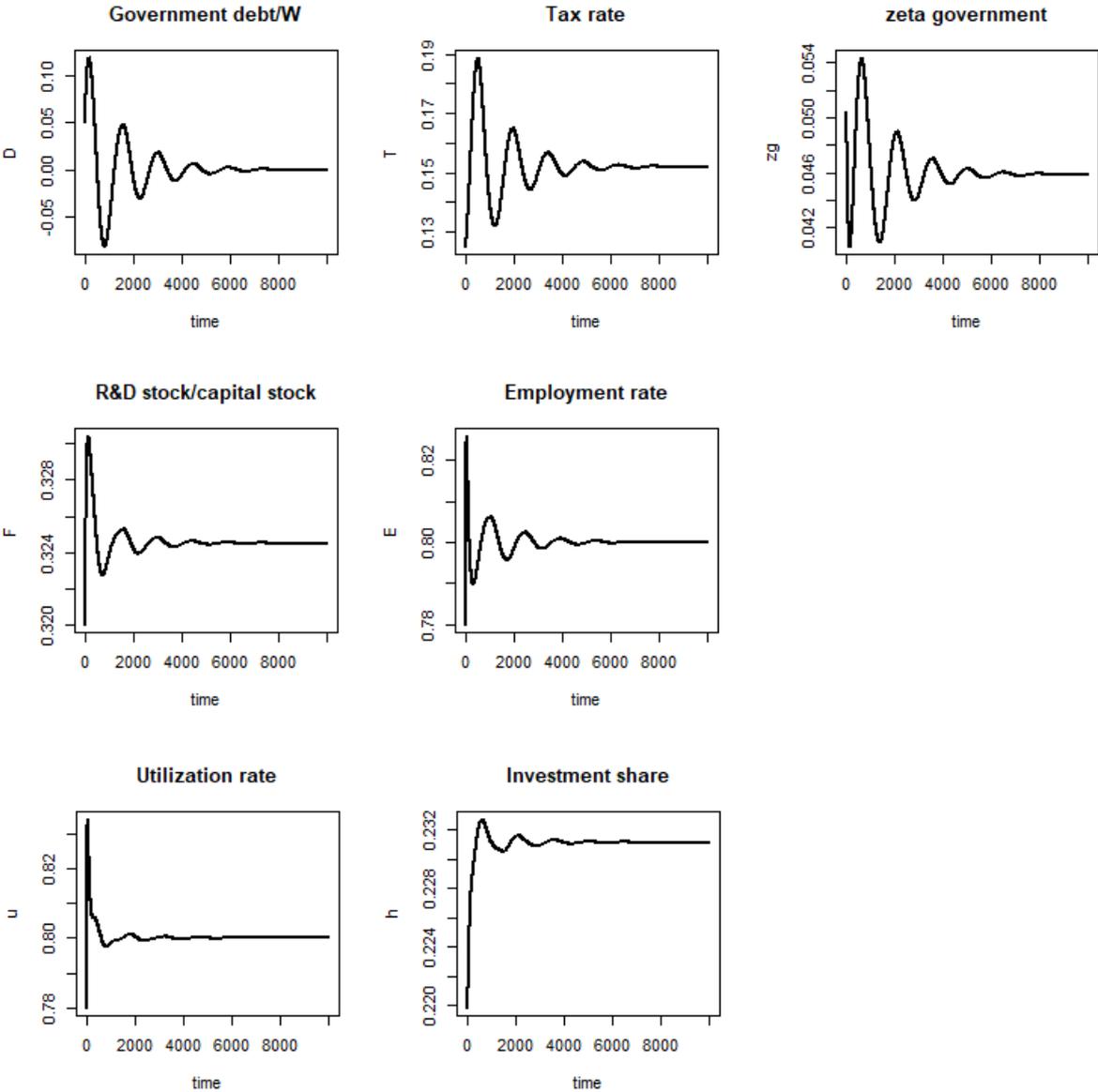
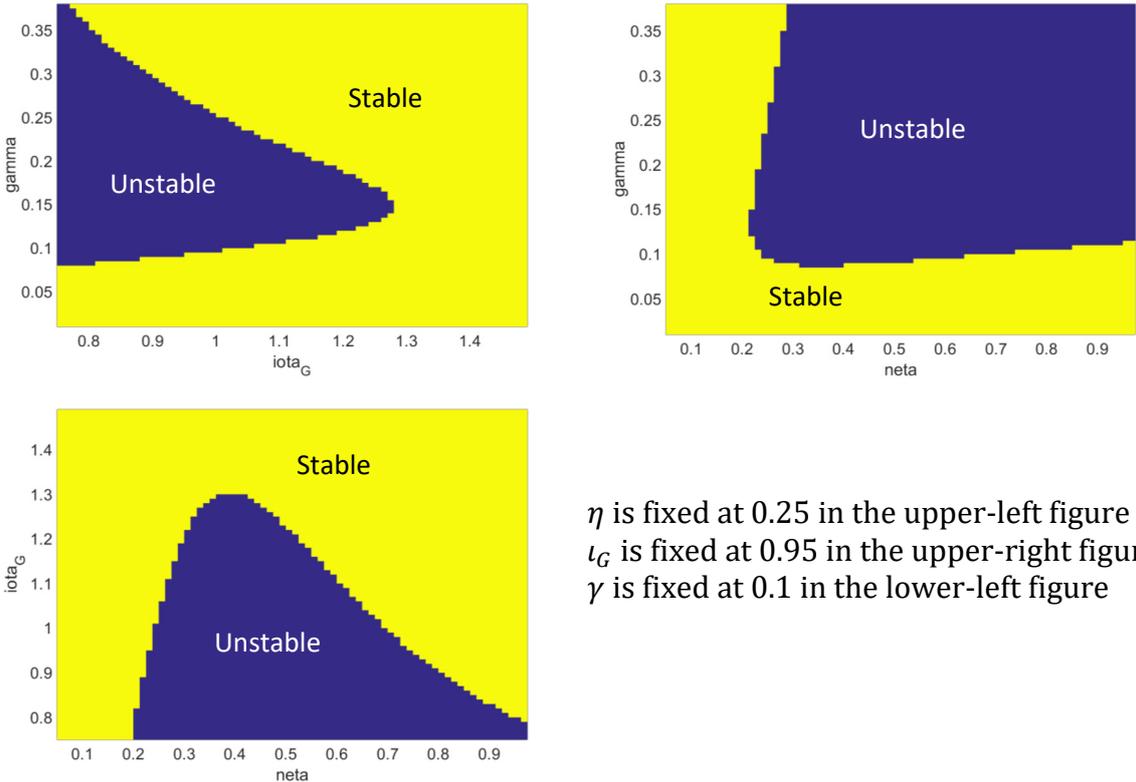


Figure 6. Government model simulation showing stability of the steady state

The stability of the steady state in the model with a government seems more precarious than the model without a government that was presented above, i.e., government stabilisation using fiscal policy is harder than with the private consumption smoothing

stabiliser in the previous sections. One of the reasons for this is that whereas before we had two adjustment parameters (γ and ι) for which we needed particular values, we now have three such adjustment parameters: η , γ and ι_G (and we also have \bar{D} , which we fixed at zero for mathematical convenience). Figure 7 presents 2D stability diagrams for each combination of two of these parameters. The underlying data for these diagrams is calculated in the same way as for the previous model, i.e., using Matlab's symbolic math module. In the next diagram, we fix the following parameters: $\tau = 0.05$, $\delta = 0.05$, $\nu = 2$, $\mu = 0.8$, $\bar{E} = 0.8$, $c = 0.6$, $\sigma = 0.7$, $\varphi = 0.1$, $\zeta_h = 0.02$ and $\bar{\rho} = 0.01$.

Focusing on γ and ι_G first (upper-left corner of the figure), we see that for low values of γ , the model is always stable, irrespective of the value of ι_G , but note that η is fixed at 0.25 (which is a fairly low value) in this diagram. Also high values of γ yield a stable steady state, but intermediate γ values require a high value for ι_G for the steady state to be stable. For the combination η and γ (in the upper-right corner), we need at least one of these two parameters to have a low value (but note that ι_G is fixed at 0.95, which is a fairly high value). Finally, for the combination of η and ι_G we see that either low or high values of η yield a stable steady state, but for intermediate values of η , we require high values of ι_G (here γ is fixed at 0.1, which is fairly low).



η is fixed at 0.25 in the upper-left figure
 ι_G is fixed at 0.95 in the upper-right figure
 γ is fixed at 0.1 in the lower-left figure

Figure 7. The role of parameters η , ι_G and γ in stability of the steady state in the government model

The rate of technological change and in particular the value of the R&D parameter τ and the private propensity to consume out of wealth (ζ_h) also have an impact on the stability

of the steady state. This is shown in Figure 8, which graphs stability in the τ vs. ζ_h plane, and where we fix $\delta = 0.05, v = 2, \mu = 0.8, \bar{E} = 0.8, c = 0.6, \sigma = 0.7, \varphi = 0.1, \eta = 0.1, \iota_G = 0.95, \gamma = 0.01$ and $\bar{\rho} = 0.01$.

Here we see a narrow band of stability emerging, which depicts a trade-off between the two parameters. High values of one of these parameters require low values of the other for the steady state to be stable, and vice versa. A combination of high ζ_h and high τ also yields negative values for the steady state of T and ζ_G , as can be seen in equations (27) and (28), and which are hard to interpret economically. Thus, the upper-right corner of instability in the figure corresponds to this counter-intuitive situation of negative taxes. The lower-left corner of instability corresponds to an economy with low growth rates (due to low R&D investment) and also low private autonomous spending.

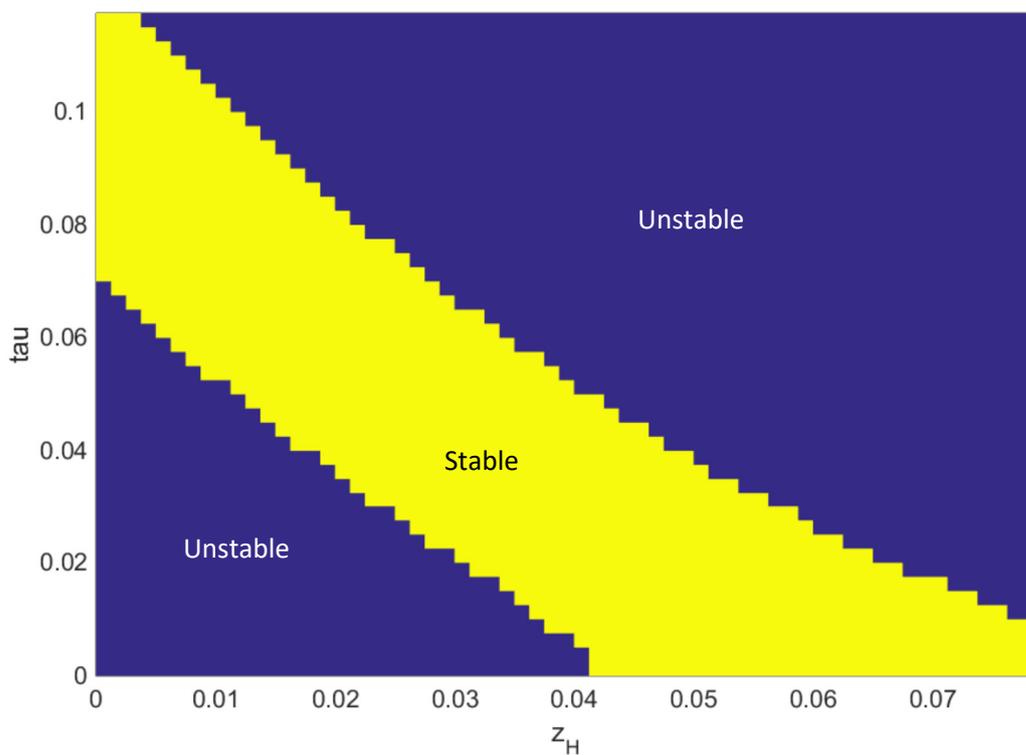


Figure 8. The role of parameters τ and ζ_h in stability of the steady state in the government model

4. Conclusions

The models that we developed in this paper confirm that a long-run steady state with economic growth generated by technological change and endogenous autonomous consumption spending can be consistent with a stable employment rate. Our model fits in the tradition of Sraffian supermultiplier Models (SSM). As we outlined above, and with

our assumption of fixed labour supply, in order to have a stable long run employment rate, autonomous consumption needs to grow at the same rate as labour productivity. Our proposal is that the equality of these two rates is obtained by consumption smoothing by wage earners (workers), who adjust their autonomous consumption spending as a fraction of their accumulated savings, in response to unemployment, and/or by government fiscal policy, where the government runs a temporary deficit (surplus) if the unemployment rate is high (low) and raises taxes to keep its long-run debt within bounds.

The (numeric) analysis of the Jacobian matrix of our models has shown that both these stabilisation mechanisms (private consumption smoothing and government fiscal policy) will keep the growth path stable, provided that certain parameter restrictions are satisfied. In the case that stabilisation takes place by workers' consumption smoothing, the ratio of the responsiveness of workers' autonomous spending to unemployment to the responsiveness of firms' investment to capital utilisation must be large enough. What this minimum value is, exactly depends on parameters in the model, such as the share of wages in GDP, R&D investment as a fraction of GDP, and the rate of autonomous consumption spending by profit earners.

In the model with government fiscal policy as the stabilisation mechanism, stability is more difficult to obtain. In this model, various parameters, including the adjustment parameters that govern fiscal policy, but also the responsiveness of firms' investment to capital utilisation, as well as the R&D intensity parameter and the propensity of the private sector to consume out of wealth, are crucial parameters that determine stability of the steady state.

Our model variety without a government includes a general consumption function, which allows for consumption spending by workers and by profit owners, and both autonomous consumption (not related to current income) and non-autonomous. Assuming that no consumption (autonomous or otherwise) is done out of profit income simplifies the steady state expressions for the variables in our model, but does not change any of the basic conclusions about growth or stability of the growth path. Also, while most of the time we assume that accumulated workers' savings earn no return, an alternative (and rudimentary) way of modelling such returns suggests that the growth path is unaffected by this (although the distribution of wealth between workers and profit earners is affected). In the model with government fiscal policy, our simplifying assumption is that the government strives for its long-run debt to be zero, and we disregard monetary policy.

We motivated our model by referring to both Schumpeter and Keynes, which represent two main factors in the growth process, respectively technological change and demand. In the resulting model, both factors indeed appear to be crucial for the emergence of a stable growth path in which we also have stable employment. Technological change (which is modelled by semi-endogenous R&D investments) relieves the resource constraint that the size of the labour force imposes on the economy, and hence makes it possible to achieve per capita growth. Endogenous demand, including endogenous autonomous consumption, keeps the economy on a path where the labour resource is used (at a fixed rate), so that the opportunities provided by technological change are actually utilised.

We feel that there are two main directions in which our model should be extended in future work. On the one hand, while we fully endogenised consumption demand, technological change was only semi-endogenised. Thus, while we considered R&D investment as a fraction of GDP as a fixed parameter, there is scope to consider it as an endogenous variable. This could be done both by making R&D dependent on other macroeconomic variables, such as (expected) profits (as in the endogenous growth literature, e.g., Aghion & Howitt, 1992), or by a behavioural approach that considers R&D at the firm level as resulting from imitation and behavioural mutation (as in Silverberg and Verspagen, 1994). Government spending may also be crucial in the field of technological change (e.g., on the Schumpeterian side of our model, as in Deleidi & Mazzucato, 2019).

On the other hand, the introduction of a more detailed way of modelling the financial sector would also enhance the degree of realism of the model. This would not only allow the modelling of the (de-)stabilising effects of finance, but also the inclusion of monetary policy by the government.

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Appendix 1. The model with generalized consumption equation

Our model with generalized consumption (and savings) behaviour starts from equation (2) in the main text, which is the consumption function:

$$C = \sigma Y c_w + (1 - \sigma) Y c_p + Z_w + Z_p \quad (2)$$

Next we define savings as any income that is not consumed, and we distinguish between savings out of labour income and out of profit income. Savings out of labour income are $S_w = \sigma Y - \sigma Y c_w - Z_w$, while savings out of profit income are $S_p = (1 - \sigma) Y - (1 - \sigma) Y c_p - Z_p$. Note that, by the usual identity, total savings are equal to total investment (R&D and fixed capital):

$$Y = \sigma Y c_w + (1 - \sigma) Y c_p + Z_w + Z_p + hY + \tau Y \Rightarrow S_w + S_p = (h + \tau) Y \quad (A1)$$

We assume that total current investment $(h + \tau) Y$ accumulates into a stock that is held by profit-earners. By slightly re-writing equation (A1) to

$$S_w = (h + \tau) Y - S_p \quad (A1')$$

we see that savings from labour income are matched by the excess of investment over savings from profit income. Although it is possible that total investment is smaller than savings from profit income, most of our analysis will focus on the case where savings out of labour income are positive, and hence investment exceeds savings out of profit income.

This implies that workers build up positive assets, and that these assets represent holdings on the profit-earning class (firms). Firms, however, also build up assets, which are the means of production (R&D capital and fixed capital), hence workers' assets represent holdings on these means of production. But capital also depreciates, which diminishes the value of the total assets of labour and profit earners together. We choose to attribute depreciation to both workers and profit earners, in proportion to total (net) assets held by each class.⁴

As was done in the main text, we assume (for mathematical convenience) that R&D capital and fixed capital depreciate at the same rate $\delta = \Delta$. This leads to the following equation for the accumulation of assets held by workers, which we denote by W_w :

$$\dot{W}_w = (1 - c_w) \sigma Y - Z_w - \delta W_w \quad (A2a)$$

The corresponding assets held by profit earners are denoted by W_p , and these accumulate according to

$$\dot{W}_p = (1 - c_p) (1 - \sigma) Y - Z_p - \delta W_p \quad (A2b)$$

Now with $Y = (Z_w + Z_p) / (1 - c_w \sigma - c_p (1 - \sigma) - \tau - h)$, equations (A2a) and (A2b) imply

$$\dot{W} = \dot{W}_w + \dot{W}_p = (h + \tau) Y - \delta (W_w + W_p) \quad (A3)$$

⁴ Alternative assumptions are possible, but make the mathematics more involved. Generally, making different assumptions about how depreciation of wealth is handled only affects the steady state distribution of wealth (x), not the growth rate.

With the initial condition $W(0) = W_w(0) + W_p(0) = R(0) + K(0)$ (the brackets indicate time periods), equation (A3) is guaranteed that $W(t) = R(t) + K(t)$ also for all times $t > 0$. In other words, total assets (wealth) available in the economy is equal to the total amount of production factors (excluding labour).

Admittedly, this means that there is essentially no, or a very limited, role for financial markets in our model. To the extent that financial markets exist, their only role is to channel savings between profit and wage earners, with the ultimate sole aim to fund the expansion of productive capacity. While here and in most of the main text we assume that there is no rate of return on the (“financial”) assets held by wage earners, in a further appendix below, we extend the treatment of financial markets to include a rate of return paid to the holders of financial assets (workers). This changes the steady state value for the distribution of wealth (x), but does not affect the growth rate of the economy.

As explained in the main text, our main assumption on autonomous spending is that it depends on wealth, i.e., the variables W_w and W_p . Allowing for autonomous consumption by both wage earners and profit earners, we stipulate

$$Z_w = \zeta_w W_w \quad (\text{A4a})$$

and

$$Z_p = \zeta_p W_p \quad (\text{A4b})$$

Note that (A4a) has also been specified in the main text. The ζ parameters are propensities to consume out of wealth for wage earners and profit earners, respectively. With the variable x defined as the share of W_w in total wealth ($W_w + W_p$), we immediately have

$$\zeta = \frac{Z}{W} = \zeta_w x + \zeta_p (1 - x) \quad (\text{A5})$$

As specified in the main text, we will assume that ζ_w is a variable, for which we specify a differential equation. On the other hand, ζ_p is assumed to be a constant parameter (and the main text assumes $\zeta_p = 0$).

With the equations specified so far, we are able to write a few of the key growth rates in the model:

$$g_W \equiv \frac{\dot{W}_w + \dot{W}_p}{W} = \frac{(1-c_w)\sigma Y - Z_w - \delta W_w + (1-c_p)(1-\sigma)Y - Z_p - \delta W_p}{W} = \zeta \left(\frac{\tau+h}{1-c_w\sigma-c_p(1-\sigma)-\tau-h} \right) - \delta \quad (\text{A6})$$

$$g_Z = \frac{\dot{W}}{W} + \frac{\dot{\zeta}}{\zeta} = \zeta \left(\frac{\tau+h}{1-c_w\sigma-c_p(1-\sigma)-\tau-h} \right) - \delta + \frac{\dot{\zeta}_w x + \zeta_w \dot{x} - \zeta_p \dot{x}}{\zeta_w x + \zeta_p (1-x)} \quad (\text{A7})$$

$$g = g_Z + \frac{\dot{h}}{1-c_w\sigma-c_p(1-\sigma)-\tau-h} \quad (\text{A8})$$

Remember that g is the growth rate of GDP.

Finally, the differential equation for x can be derived as follows:

$$\dot{x} = \frac{\dot{W}_w}{W_w + W_p} - \frac{W_w(\dot{W}_w + \dot{W}_p)}{(W_w + W_p)^2} = \frac{(\zeta_w x + \zeta_p(1-x))((1-c_w)\sigma - x(\tau+h))}{1-c_w\sigma-c_p(1-\sigma)-\tau-h} - \zeta_w x \quad (\text{A9})$$

We can also summarize the other five (in addition to A9) differential equations that make up the model with the generalized consumption function (equation numbers refer to the main text, and remember $\Delta = \delta$):

$$\dot{h} = h\gamma(u - \mu) \quad (1)$$

$$\dot{\Phi} = \Phi \frac{u}{v} \left(\frac{\tau}{\Phi} - h \right) \quad (11)$$

$$\dot{\zeta}_w = \iota \zeta_w (\bar{E} - E) \quad (13)$$

$$\dot{u} = u \left(\frac{(\zeta_w x + \zeta_p (1-x))(\tau+h)+\dot{h}}{1-c_w \sigma - c_p (1-\sigma) - \tau - h} + \frac{\zeta_w \dot{x} + \zeta_p \dot{x} - \zeta_p \dot{x}}{\zeta_w x + \zeta_p (1-x)} - \frac{hu}{v} \right) \quad (A10)$$

$$\dot{E} = E \left(\frac{(\zeta_w x + \zeta_p (1-x))(\tau+h)+\dot{h}}{1-c_w \sigma - c_p (1-\sigma) - \tau - h} + \frac{\zeta_w \dot{x} + \zeta_p \dot{x} - \zeta_p \dot{x}}{\zeta_w x + \zeta_p (1-x)} - \delta - \bar{\rho} - \varphi \Phi \right) \quad (A11)$$

These equations can be solved for the steady state of the model using the procedure outlined in the main text. The steady state expressions presented in the main text are specific for the assumptions $c_p = 0$ and $\zeta_p = 0$. The generalized steady state expressions for u , E , Φ and h are identical to the expressions in the main text. The generalized steady state expressions for the two remaining variables are

$$x^* = \frac{v(1+\Phi^*)(\zeta_p + \delta + \bar{\rho} + \varphi \Phi^*) - \mu s_p (1-\sigma)}{v(1+\Phi^*)(\zeta_p + \delta + \bar{\rho} + \varphi \Phi^*)} \quad (A12)$$

$$\zeta_w^* = \frac{[\mu(\sigma s_w + (1-\sigma)s_p) - v(\delta + \bar{\rho} + \varphi \Phi)(1+\Phi^*)](\zeta_p + \delta + \bar{\rho} + \varphi \Phi^*) - \zeta_p \mu s_p (1-\sigma)}{v(1+\Phi^*)(\zeta_p + \delta + \bar{\rho} + \varphi \Phi^*) - \mu s_p (1-\sigma)} \quad (A13)$$

In these expressions, we substituted the definitions $s_p \equiv 1 - c_p$ and $s_w \equiv 1 - c_w$.

Appendix 2. Introducing a rate of return to workers' assets

As explained in the main text, we model the rate of return on accumulated workers' savings by the introduction of a parameter r , which represents the fraction of profits that is paid to workers in return for their savings, which are used by firms (profit earners) to pay for the investments in fixed capital and R&D. With the inclusion r into the model, workers will receive a share $\sigma + rx(1 - \sigma)$ of GDP, and profits earners a share $(1 - \sigma)(1 - rx)$. This changes the equations (equations A2a and A2b) for accumulation of wealth:

$$\dot{W}_w = s_w(\sigma + rx(1 - \sigma))Y - \zeta_w W_w - \delta W_w \quad (A2a')$$

$$\dot{W}_p = s_p(1 - \sigma)(1 - rx)Y - \zeta_p W_p - \delta W_p \quad (A2b')$$

It also changes the multiplier, as can be seen in the equation for output:

$$Y = Z_w + Z_p + c_w(\sigma + rx(1 - \sigma))Y + c_p((1 - \sigma)(1 - rx))Y + (h + \tau)Y \Rightarrow$$

$$Y = \frac{Z_w + Z_p}{1 - c_w(\sigma + rx(1 - \sigma)) - c_p((1 - \sigma)(1 - rx)) - (h + \tau)} \quad (3a')$$

Note that in this equation, we have assumed that the marginal propensity to consume out of current income is unchanged, both for workers and profit earners, even if with $r > 0$, workers' income is partly profits (or returns on savings).

From these basic changes associated to the introduction of r , the differential equations of the model can be derived in the same way as before. We find that three equations change, specifically:

$$\dot{u} = u \left(\frac{(\zeta_w x + \zeta_p(1-x))(h+\tau) + \dot{h} - \dot{x}(1-\sigma)(s_p - s_w)}{1 - (1-s_w)(\sigma + rx(1-\sigma)) - (1-s_p)(1-rx)(1-\sigma) - (h+\tau)} + \frac{\zeta_w \dot{x} + \zeta_p \dot{x} - \zeta_p \dot{x}}{\zeta_w x + \zeta_p(1-x)} - \frac{hu}{v} \right) \quad (\text{A10}')$$

$$\dot{E} = E \left(\frac{(\zeta_w x + \zeta_p(1-x))(h+\tau) + \dot{h} - \dot{x}(1-\sigma)(s_p - s_w)}{1 - (1-s_w)(\sigma + rx(1-\sigma)) - (1-s_p)(1-rx)(1-\sigma) - (h+\tau)} + \frac{\zeta_w \dot{x} + \zeta_p \dot{x} - \zeta_p \dot{x}}{\zeta_w x + \zeta_p(1-x)} - \delta - \bar{\rho} - \varphi\Phi \right) \quad (\text{A11}')$$

$$\dot{x} = \frac{(\zeta_w x + \zeta_p(1-x))[s_w(\sigma + rx(1-\sigma)) - x(h+\tau)]}{1 - (1-s_w)(\sigma + rx(1-\sigma)) - (1-s_p)(1-rx)(1-\sigma) - (h+\tau)} - \zeta_w x \quad (\text{A9}')$$

This model (which also includes equations 1, 11 and 13) can be solved for the steady state in essentially the same way as has been done for the case $r = 0$. Related to the fact that in equations (A10') and (A11'), the parameter r only appears in the multiplier (as in A3a'), the steady state solutions for h and Φ do not change. With equations (1) and (13) unchanged, the steady state solutions for u and E also do not change. Thus, we obtain only steady state expressions for x^* and ζ_w^* that are different than before, while the other steady state expressions do not change:

$$x^* = \frac{\frac{u}{v} s_p(1-\sigma) - (1+\Phi^*)(\zeta_p + \delta + \bar{\rho} + \varphi\Phi^*)}{\frac{u}{v} s_p(1-\sigma)r - (1+\Phi^*)(\zeta_p + \delta + \bar{\rho} + \varphi\Phi^*)} \quad (\text{A14})$$

$$\zeta_w^* = \frac{\mu}{v} \frac{(s_w - s_p)r(1-\sigma)}{(1+\Phi^*)} + \frac{\frac{\mu}{v}(s_w\sigma + s_p(1-\sigma)) - (1+\Phi^*)(\delta + \bar{\rho} + \varphi\Phi^*)}{(1+\Phi^*)} \frac{1}{x^*} - \zeta_p \frac{\frac{\mu}{v} s_p(1-\sigma)(1-r)}{\frac{\mu}{v} s_p(1-\sigma) - (1+\Phi^*)(\zeta_p + \delta + \bar{\rho} + \varphi\Phi^*)} \quad (\text{A15})$$

Especially the expression for ζ_w^* is rather complicated. However, it can easily be seen that with $r = 0$ it reduces to equation (A13). Similarly, equation (A14) reduces to (A12) for the case $r = 0$. We can also reduce these steady state expressions for the case $r = 1$:

$$x^* = 1 \quad (\text{A16})$$

$$\zeta_w^* = \frac{\mu}{v(1+\Phi^*)} s_w - (\delta + \bar{\rho} + \varphi\Phi^*) \quad (\text{A17})$$

Appendix 3. Details of the government stabilization model

There are a number of equations that change slightly in the model with a government sector. This appendix presents the details of these equations. First, the introduction of taxes implies that consumption is a function of disposable income:

$$C = Z_H + c(1 - T + (1 - \sigma)D)Y \quad (\text{2a})$$

Using also the definitions that are specified in the main text, this leads to the following equation for GDP:

$$Y = (Z_H + Z_G) \frac{1}{1-c(1-T+(1-\sigma)D)-(h+\tau)} \quad (3b)$$

Because government bonds are held by private agents (any increase of G will correspond to a private surplus), total assets held by private agents are equal to $W + G$. This modifies the equation for private autonomous spending to

$$Z_h = \zeta_h(W + G) \quad (A4c)$$

The equation for government autonomous spending is specified in the main text (A4d), and together these two equations lead to

$$Z = Z_G + Z_h = (\zeta_G + \zeta_h)W + \zeta_h G \quad (A4e)$$

In line with our previous derivations (Appendix 1), we also have

$$\frac{\dot{W}}{W} = \frac{(h+\tau)[(\zeta_H+\zeta_G)+\zeta_H D]}{1-c(1-t+(1-\sigma)D)-(h+\tau)} - \delta \quad (A3b)$$

And from equations (23) and (2a) as well as the definition of D , it follows that

$$\frac{\dot{G}}{G} = \frac{1}{D} \left[\zeta_G + \frac{((1-\sigma)D-t)[(\zeta_H+\zeta_G)+\zeta_H D]}{1-c(1-t+(1-\sigma)D)-(h+\tau)} \right] \quad (A18)$$

Then it can easily be seen that

$$g_Z = \frac{\dot{z}_g - (\zeta_H + \zeta_G)\delta + \zeta_H \zeta_G}{(\zeta_H + \zeta_G) + \zeta_H D} + \frac{(\zeta_H + \zeta_G)(h+\tau) + \zeta_H((1-\sigma)D-t)}{1-c(1-t+(1-\sigma)D)-(h+\tau)} \quad (A7a)$$

With this new equation for g_Z , we also have new equations for \dot{u} and \dot{E} :

$$\dot{u} = u \left(\frac{\dot{z}_g - (\zeta_H + \zeta_G)\delta + \zeta_H \zeta_G}{(\zeta_H + \zeta_G) + \zeta_H D} + \frac{(\zeta_H + \zeta_G)(h+\tau) + \zeta_H((1-\sigma)D-t) - ct + c(1-\sigma)\dot{D} + \dot{h}}{1-c(1-t+(1-\sigma)D)-(h+\tau)} - \frac{hu}{v} + \delta \right) \quad (7a)$$

$$\dot{E} = E \left(\frac{\dot{z}_g - (\zeta_H + \zeta_G)\delta + \zeta_H \zeta_G}{(\zeta_H + \zeta_G) + \zeta_H D} + \frac{(\zeta_H + \zeta_G)(h+\tau) + \zeta_H((1-\sigma)D-t) - ct + c(1-\sigma)\dot{D} + \dot{h}}{1-c(1-t+(1-\sigma)D)-(h+\tau)} - \bar{\rho} - \varphi\Phi \right) \quad (8a)$$

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